

BIBLIOGRAPHY ON HILBERT SCHEMES

This is a partial bibliography on Hilbert schemes. Omissions probably outnumber inclusions - email bibtex entries of the most egregious to `D.Maclagan@warwick.ac.uk` to join the long list of contributors.

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